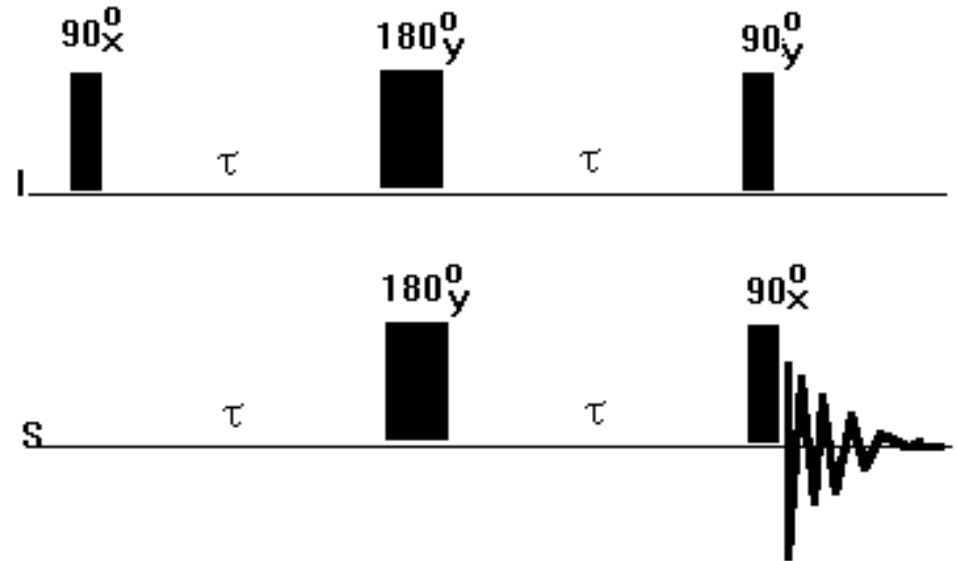


INEPT = Insensitive Nuclei Enhanced by Polarization Transfer

Heteronuclear I, S

Consider: Ω_I , Ω_S and J_{IS}
 (I and S are heteronuclear)



The pulse sequence:

(e.g. ^1H)

I: 90°_x ----- τ ----- 180°_y ----- τ ----- 90°_y

(e.g. ^{13}C)

S: ----- τ ----- 180°_y ----- τ ----- 90°_x ACQ
 -----e c h o -----

$\tau = 1/(4J_{IS})$ e.g. $J_{\text{CH}} = 150 \text{ Hz} \rightarrow \tau = 1.67 \text{ ms}$

$a \approx 4b$ (the intensity (γ) difference between spin I and S)

$\sigma[\text{eq.}]$

$\hat{H} = \pi/2 (\hat{I}_x)$

$\sigma[0]$

$a\mathbf{I}_z$ and $b\mathbf{S}_z$

$\downarrow 90^\circ_x$

$-a\mathbf{I}_y$ and $b\mathbf{S}_z$

memo : this is a spin-echo (180° on I and S „homo“-like situation)

coupling evolves but chemical shift doesn't evolve

$$\hat{H} = 2\hat{I}_z\check{S}_z(J_{IS}\pi\tau)$$

$$\downarrow$$

$$-a\mathbf{I}_y \cos(\pi J_{IS}\tau) + a2\mathbf{I}_x\mathbf{S}_z \sin(\pi J_{IS}\tau)$$

$$\hat{H} = \pi\hat{I}_y$$

$$b\mathbf{S}_z$$

$$\downarrow$$

$$-a\mathbf{I}_y \cos(\pi J_{IS}\tau) - a2\mathbf{I}_x\mathbf{S}_z \sin(\pi J_{IS}\tau)$$

$$\hat{H} = \pi\mathbf{S}_y$$

$$b\mathbf{S}_z$$

$$\downarrow$$

$$-a\mathbf{I}_y \cos(\pi J_{IS}\tau) + a2\mathbf{I}_x\mathbf{S}_z \sin(\pi J_{IS}\tau)$$

$$\hat{H} = 2\hat{I}_z\check{S}_z(J_{IS}\pi\tau)$$

$$-b\mathbf{S}_z$$

$$\downarrow$$

$$-a\mathbf{I}_y \cos(\pi J_{IS}\tau)\cos(\pi J_{IS}\tau) + a2\mathbf{I}_x\mathbf{S}_z \cos(\pi J_{IS}\tau)\sin(\pi J_{IS}\tau) + a2\mathbf{I}_x\mathbf{S}_z \sin(\pi J_{IS}\tau)\cos(\pi J_{IS}\tau) + a\mathbf{I}_y \sin(\pi J_{IS}\tau)\sin(\pi J_{IS}\tau)$$

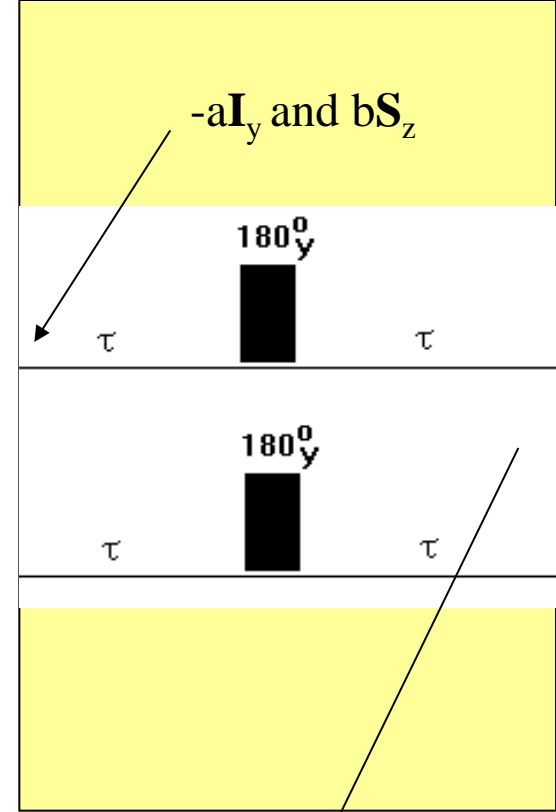
$$-b\mathbf{S}_z$$

memo 1: $\cos^2 A - \sin^2 A = \cos 2A$

$$-a\mathbf{I}_y \{ \cos(\pi J_{IS}\tau)\cos(\pi J_{IS}\tau) - \sin(\pi J_{IS}\tau)\sin(\pi J_{IS}\tau) \} = -a\mathbf{I}_y \cos(2\pi J_{IS}\tau)$$

memo 2: $2\cos A \sin A = \sin 2A$

$$2\{ +a2\mathbf{I}_x\mathbf{S}_z \sin(\pi J_{IS}\tau)\cos(\pi J_{IS}\tau) \} = +a2\mathbf{I}_x\mathbf{S}_z \sin(2\pi J_{IS}\tau)$$



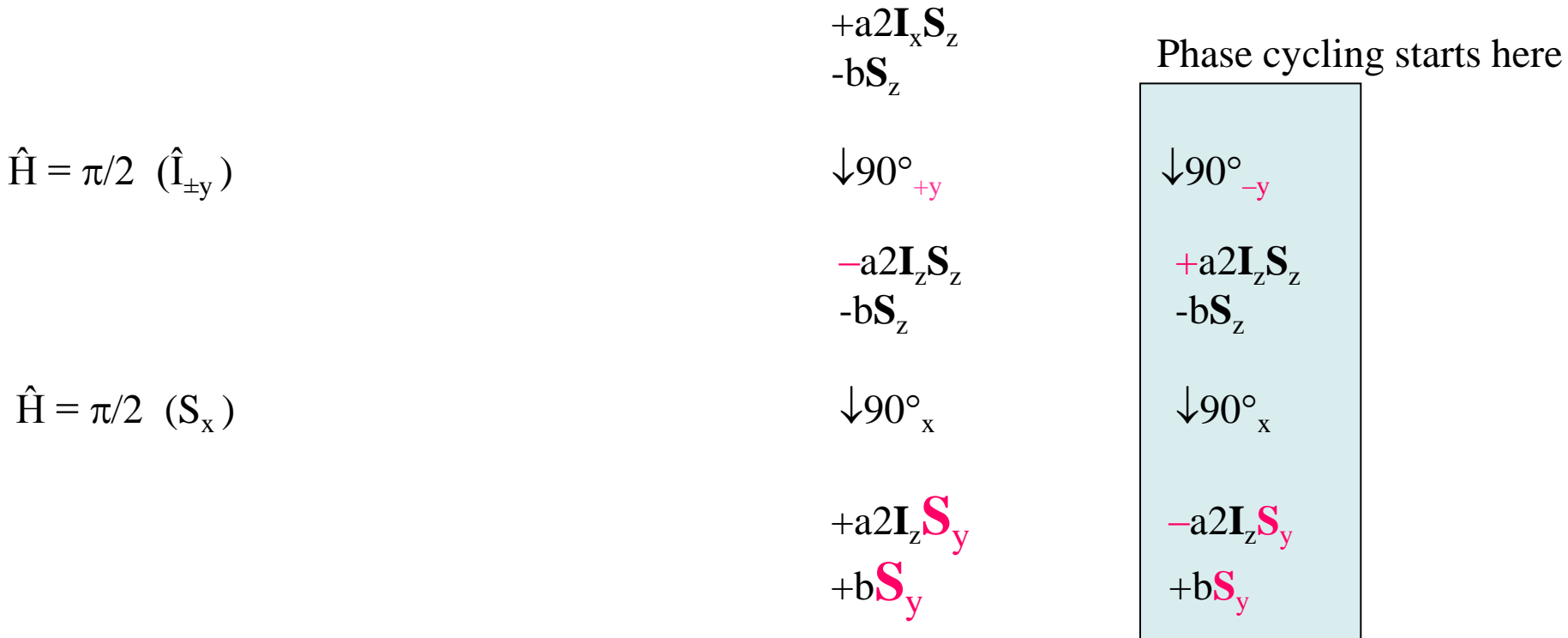
Therefore the

$$-a\mathbf{I}_y \cos(2\pi J_{IS}\tau) + a2\mathbf{I}_x\mathbf{S}_z \sin(2\pi J_{IS}\tau)$$

$$-b\mathbf{S}_z$$

terms remain.

since $\tau = 1/(4J_{IS}) \rightarrow \cos(2\pi J_{IS}\tau)=0$ and $\sin(2\pi J_{IS}\tau)=1$



Both terms are **magnetization on spin S**

- 1) $+a2\mathbf{I}_z\mathbf{S}_y$: anti-phased magnetization on spin S with intensity factor of spin I.
- 2) $+b\mathbf{S}_y$: in phased magnetization on spin S.

The first term during ACQ :

$$+a2\mathbf{I}_z\mathbf{S}_y$$

$$\hat{H} = \mathbf{S}_z(\Omega_S[t_2])$$

$$\hat{H} = 2\hat{\mathbf{I}}_z\check{\mathbf{S}}_z(\mathbf{J}_{IS}\pi[t_2])$$

↓

$$\begin{aligned}
 &+a2\mathbf{I}_z\mathbf{S}_y \cos(\Omega_S t_2) \cos(\pi\mathbf{J}_{IS} t_2) \\
 &\quad -a\mathbf{S}_x \cos(\Omega_S t_2) \sin(\pi\mathbf{J}_{IS} t_2) \\
 &\quad -a2\mathbf{I}_z\mathbf{S}_x \sin(\Omega_S t_2) \cos(\pi\mathbf{J}_{IS} t_2) \\
 &\quad \quad -a\mathbf{S}_y \sin(\Omega_S t_2) \sin(\pi\mathbf{J}_{IS} t_2)
 \end{aligned}$$

memo 1: put the receiver on x

therefore only the single x term remain : $-a\mathbf{S}_x \cos(\Omega_S t_2) \sin(\pi\mathbf{J}_{IS} t_2)$

memo 2: $\cos(A)\sin(B) = 1/2[\sin(A+B)-\sin(A-B)]$

therefore $-a\mathbf{S}_x 1/2[+\sin\{(\Omega_S+\pi\mathbf{J}_{IS})t_2\}-\sin\{(\Omega_S-\pi\mathbf{J}_{IS})t_2\}]$

the following terms can be found:

$$-a\mathbf{S}_x 1/2[+ \dots - \dots] \text{ at } \Omega_S$$

setting the phase that *sin* is absorptive :

$$-a\mathbf{S}_x 1/2[+a .. -a ..] \text{ at } \Omega_S$$

remark: an antiphase doublet ($^1,^1\mathbf{J}[\text{H},\text{N}] \cong 90 \text{ Hz}$, $^1,^1\mathbf{J}[\text{H},\text{C}] \cong 150 \text{ Hz}$) is observed.

*conclusion: The spectrum is an antiphase doublet at Ω_S of an **enhanced intensity**.*

The second term during ACQ :

$$+b\mathbf{S}_y$$

$$\hat{H} = S_z(\Omega_S[t_2])$$

↓

$$\hat{H} = 2\hat{I}_z \check{S}_z(\mathbf{J}_{IS}\pi[t_2])$$

$$\begin{aligned}
 &+b\mathbf{S}_y \cos(\Omega_S t_2) \cos(\pi \mathbf{J}_{IS} t_2) \\
 &\quad -b2\mathbf{I}_z \mathbf{S}_x \cos(\Omega_S t_2) \sin(\pi \mathbf{J}_{IS} t_2) \\
 &\quad -b\mathbf{S}_x \sin(\Omega_S t_2) \cos(\pi \mathbf{J}_{IS} t_2) \\
 &\quad \quad -b2\mathbf{I}_z \mathbf{S}_y \sin(\Omega_S t_2) \sin(\pi \mathbf{J}_{IS} t_2)
 \end{aligned}$$

memo 1: we placed the receiver on x

therefore only the single x term remains: $-b\mathbf{S}_x \sin(\Omega_S t_2) \cos(\pi \mathbf{J}_{IS} t_2)$

memo 2: $\sin(A)\cos(B) = 1/2[\sin(A+B) + \sin(A-B)]$

therefore

$$-b\mathbf{S}_x 1/2[+\sin\{(\Omega_S + \pi \mathbf{J}_{IS})t_2\} + \sin\{(\Omega_S - \pi \mathbf{J}_{IS})t_2\}]$$

the following terms can be found:

$$-b\mathbf{S}_x 1/2[+ \dots + \dots] \text{ at } \Omega_S$$

we have set the phase that *sin* is absorptive :

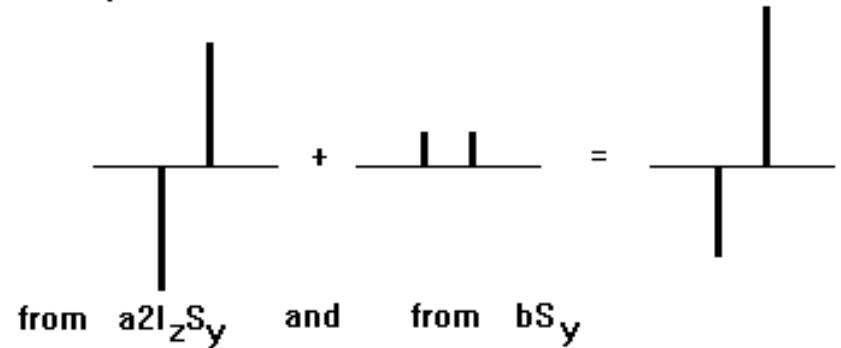
$$-b\mathbf{S}_x 1/2[+a .. +a ..] \text{ at } \Omega_S$$

the two terms are the following:

$$-a\mathbf{S}_x \frac{1}{2} [+\sin\{(\Omega_S + \pi J_{IS})t_2\} - \sin\{(\Omega_S - \pi J_{IS})t_2\}]$$

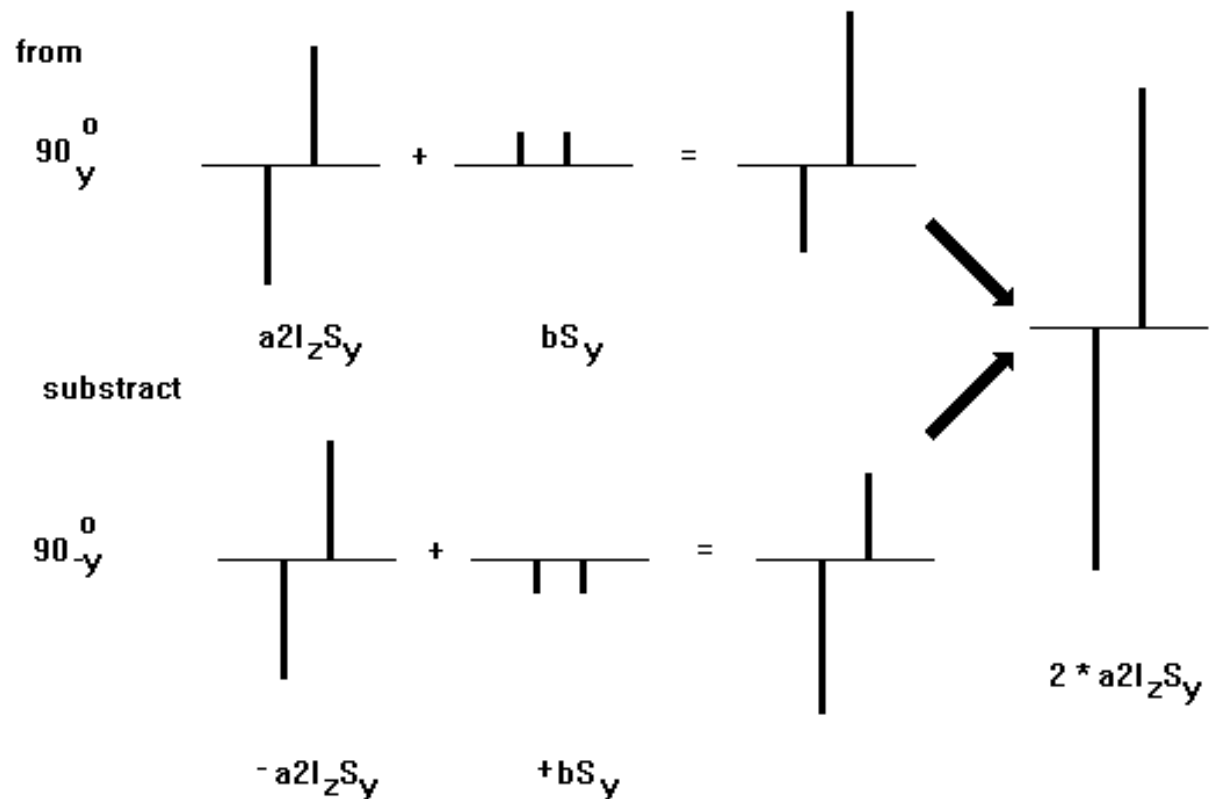
$$-b\mathbf{S}_x \frac{1}{2} [+\sin\{(\Omega_S + \pi J_{IS})t_2\} + \sin\{(\Omega_S - \pi J_{IS})t_2\}]$$

the spectrum



The second term can be phase-cycled out (2 step phase cycle).

Therefore, the two $+a2I_zS_y$ remain.



What does the INEPT module do?

Heteronuclear I, S,
with Ω_I , Ω_S and J_{IS}

An INEPT module
makes from in-
phased I an anti-
phased S coherence.
But with the
coherence transfer
„the sensitivity
(a)“ of spin I is also
transferred!!!

Compare to a simple 90_x^0 :

